



# High Speed Optical Networking: Task 3 FEC Coding, Channel Models, and Evaluations

**Joel M. Morris, PhD**

Communications and Signal Processing Laboratory (CSPL)

UMBC/CSEE Department

1000 Hilltop Circle, Catonsville, MD 21250

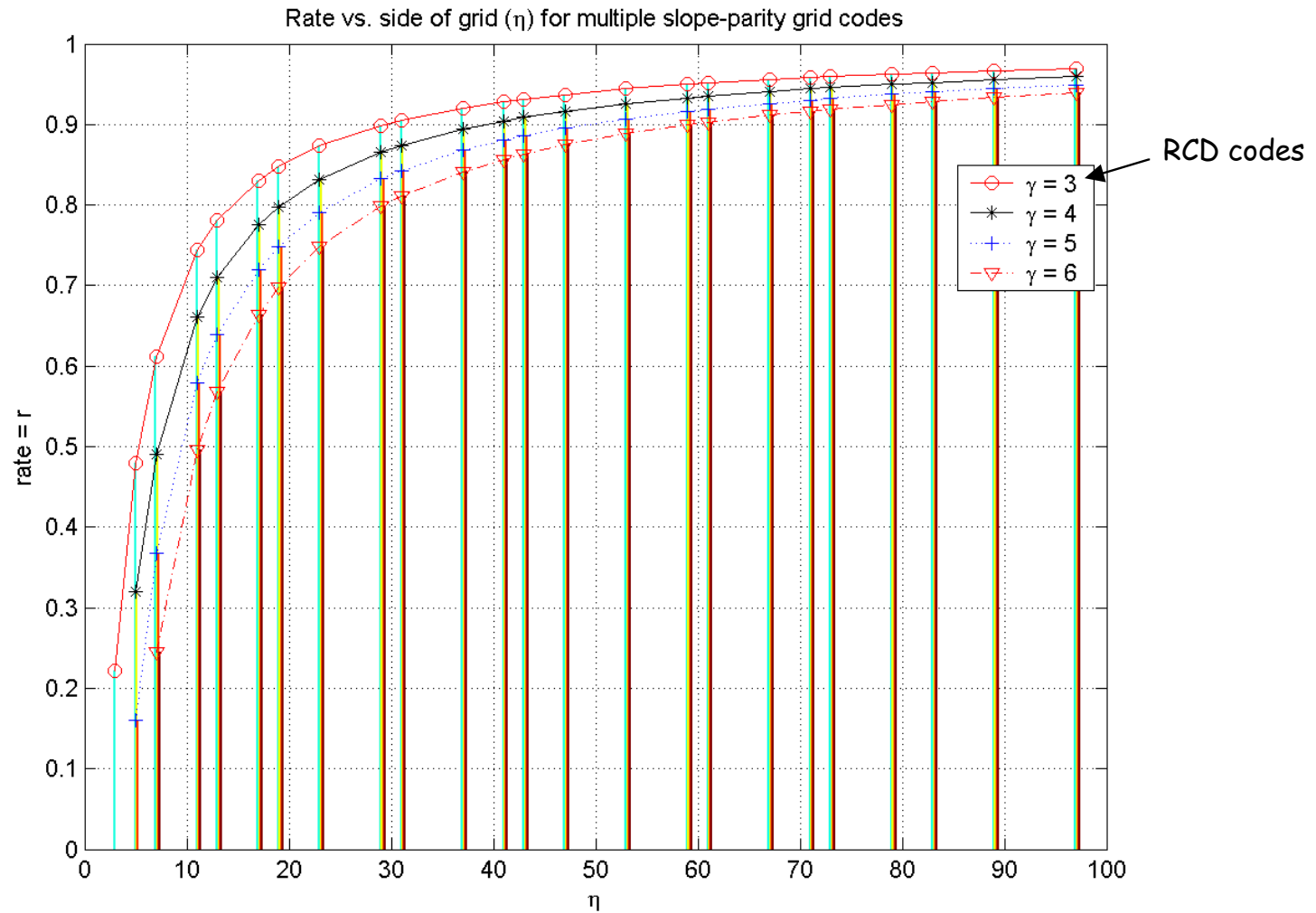
morris@umbc.edu 410.455.3503

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# FEC Coding: RCD Codes

- Subset of Regular LDPC Codes
- Decodable via Variety of Decoder Schemes
  - w/ Choice Driven by Performance vs. Technology Trade-offs
  - Majority-Logic (MLG) Decoding
  - Iterative Hard-Decision Decoding (Bit-Flipping)
  - Iterative Soft-Decision Decoding (SPA)
- High Code Rates (Low Overhead) Possible
- Weakly Random-like

# Multiple slope-parity codes code-rate vs $\eta$



# FEC Coding

## Weight enumerator function (WEF) for RCD Codes

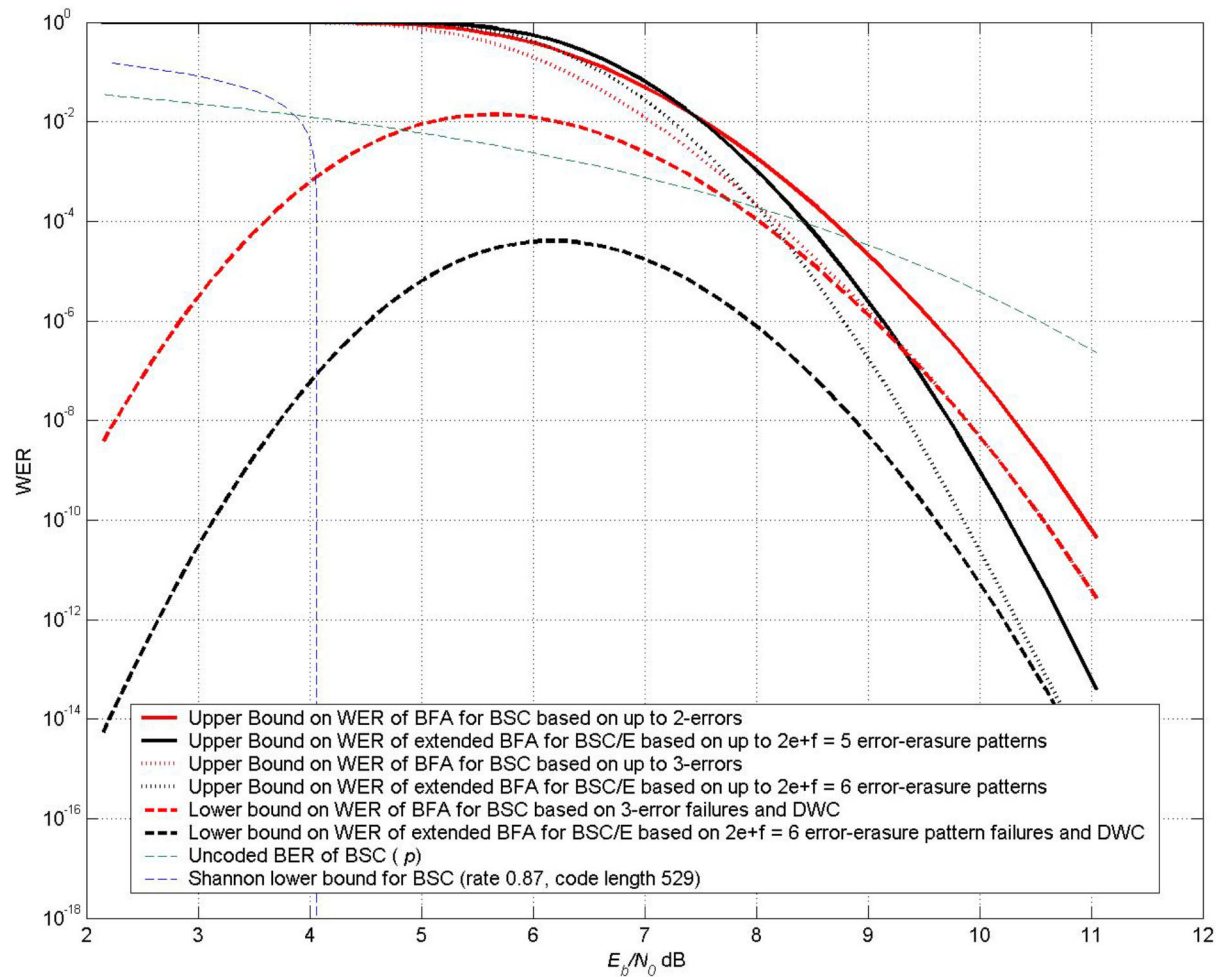
➡ WER/BER performance bounds

- Upper & lower bounds on BDD for BSC
- Union bound as upper bound on ML decoding

## BFA decoding of RCD codes for decoding 3 & 4 error patterns on BSC

- Exhaustive enumeration and classification of 3 & 4 error patterns for various  $\eta$ 
  - ➡ Expression conjectured for 3 errors,  $\forall \eta$
- FPGA design of BFA for (255,175) LDPC code

## WER performance bounds for $\eta=23$ RCD code under BFA for BSC and EBFA for BSC/E



# Channel Models

BAC model  $\sim$  chi-squared *pdf* based

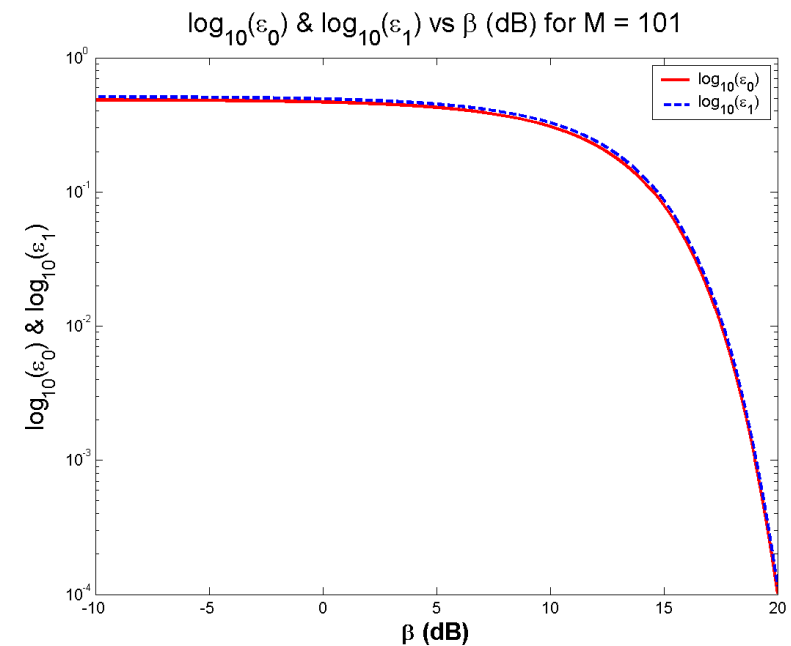
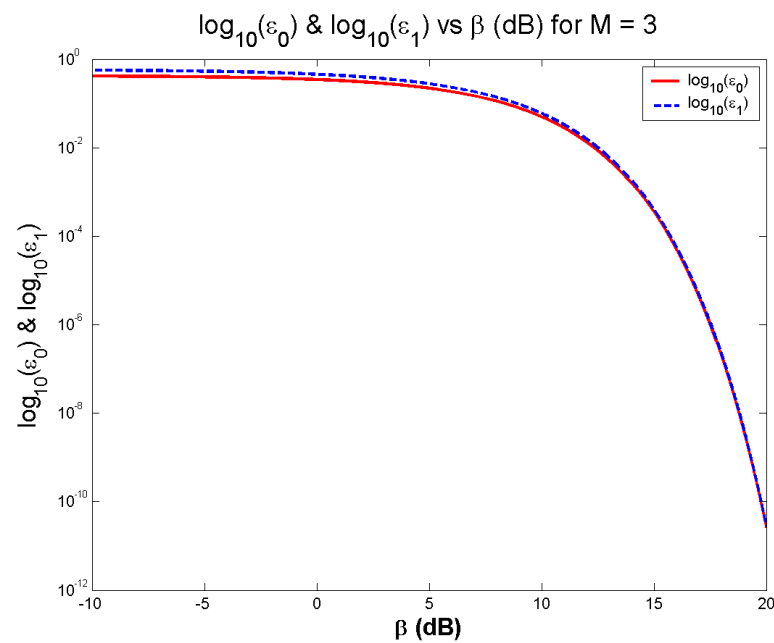
- Shannon limit expression & plots
- Channel capacity expressions & plots
- WER lower bound curves & plots
- Optimal crossover errors close to BSC errors  $\forall M$
- BSC model obtained via threshold settings

BSC/E model yields significant improvement over BSC

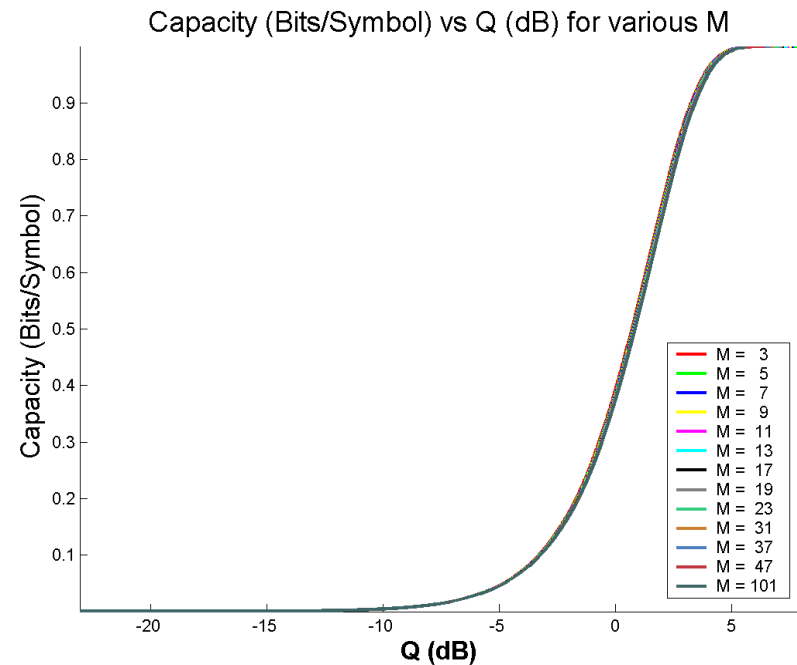
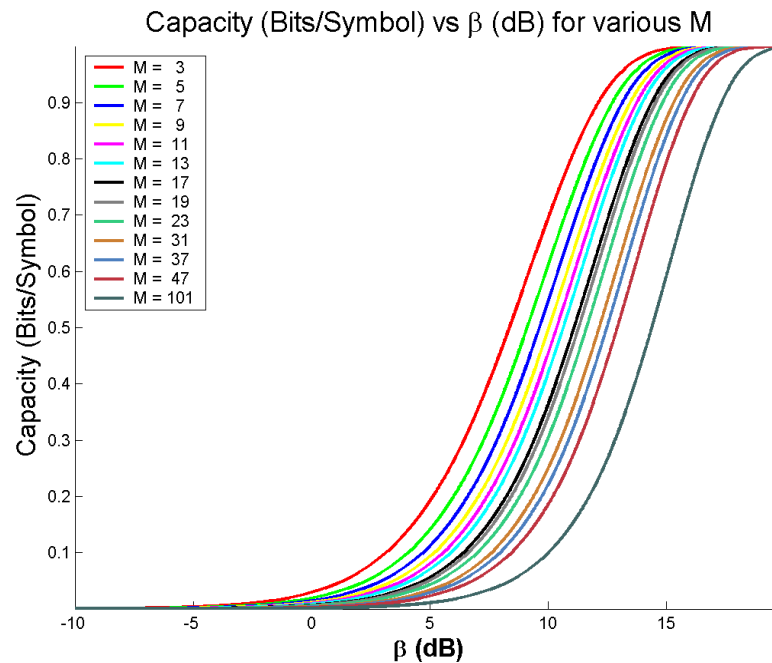
- Using EBFA on BSC/E for RCD codes
- Using extended BDD on BSC/E for LDPC codes
- Channel capacity and Shannon limit comparisons w/BSC

## BAC transition probabilities $\varepsilon_0$ and $\varepsilon_1$ vs $\beta$ for $M = 3$ and $M = 101$

$$\beta = R_c E_b / N_o$$



# BAC capacity vs $\beta$ and $Q$ for various $M$



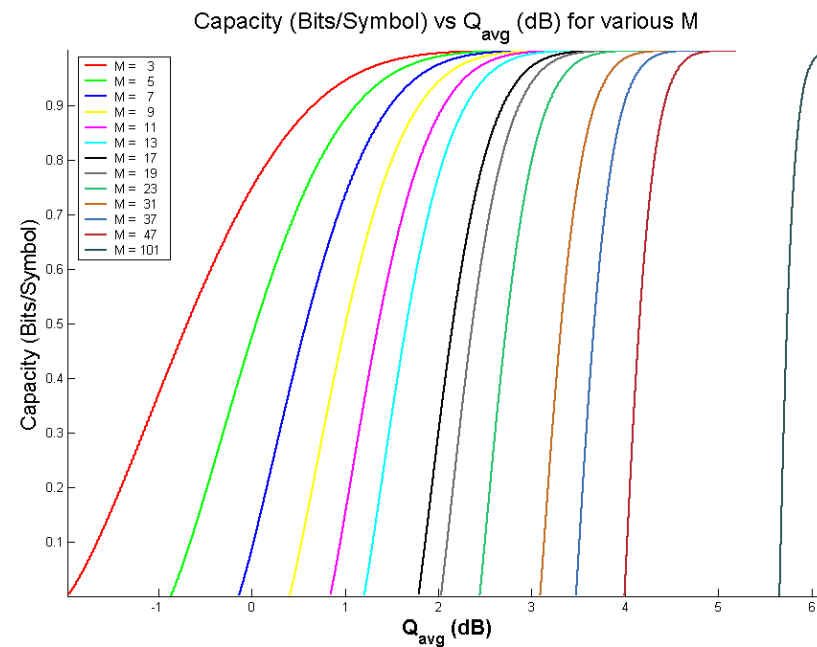
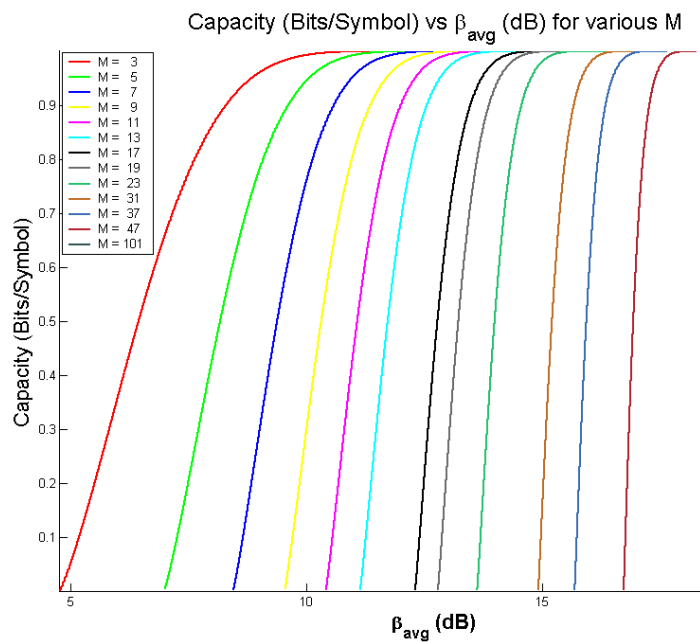
$$\beta = R_c E_b / N_o$$

$$Q = (\mu_1 - \mu_0) / (\sigma_1 + \sigma_0) = \beta / (\sqrt{M} + \sqrt{M + 2\beta})$$

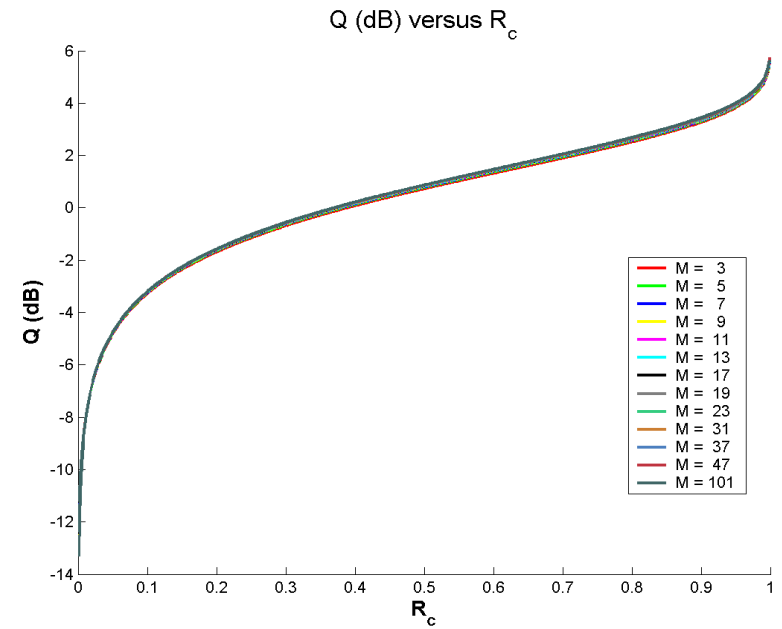
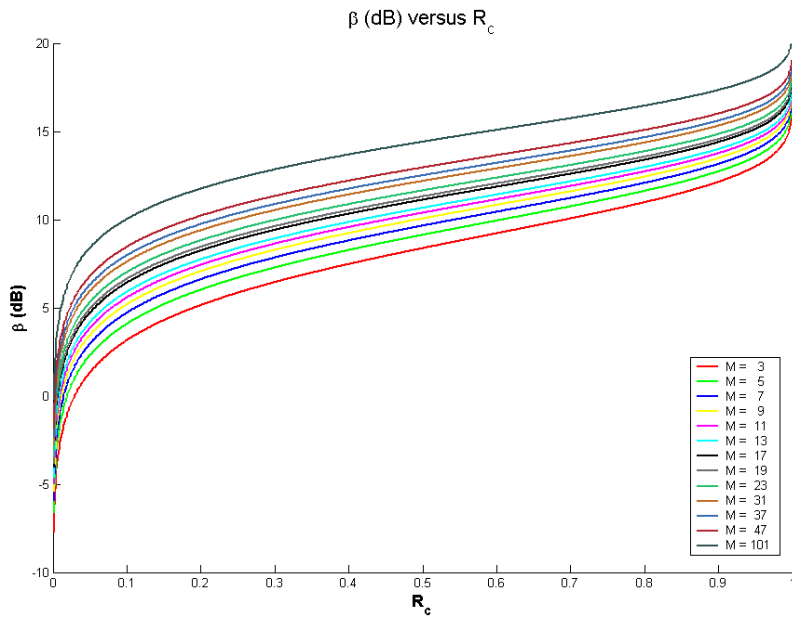


## BAC capacity vs $\beta_{avg}$ for various M

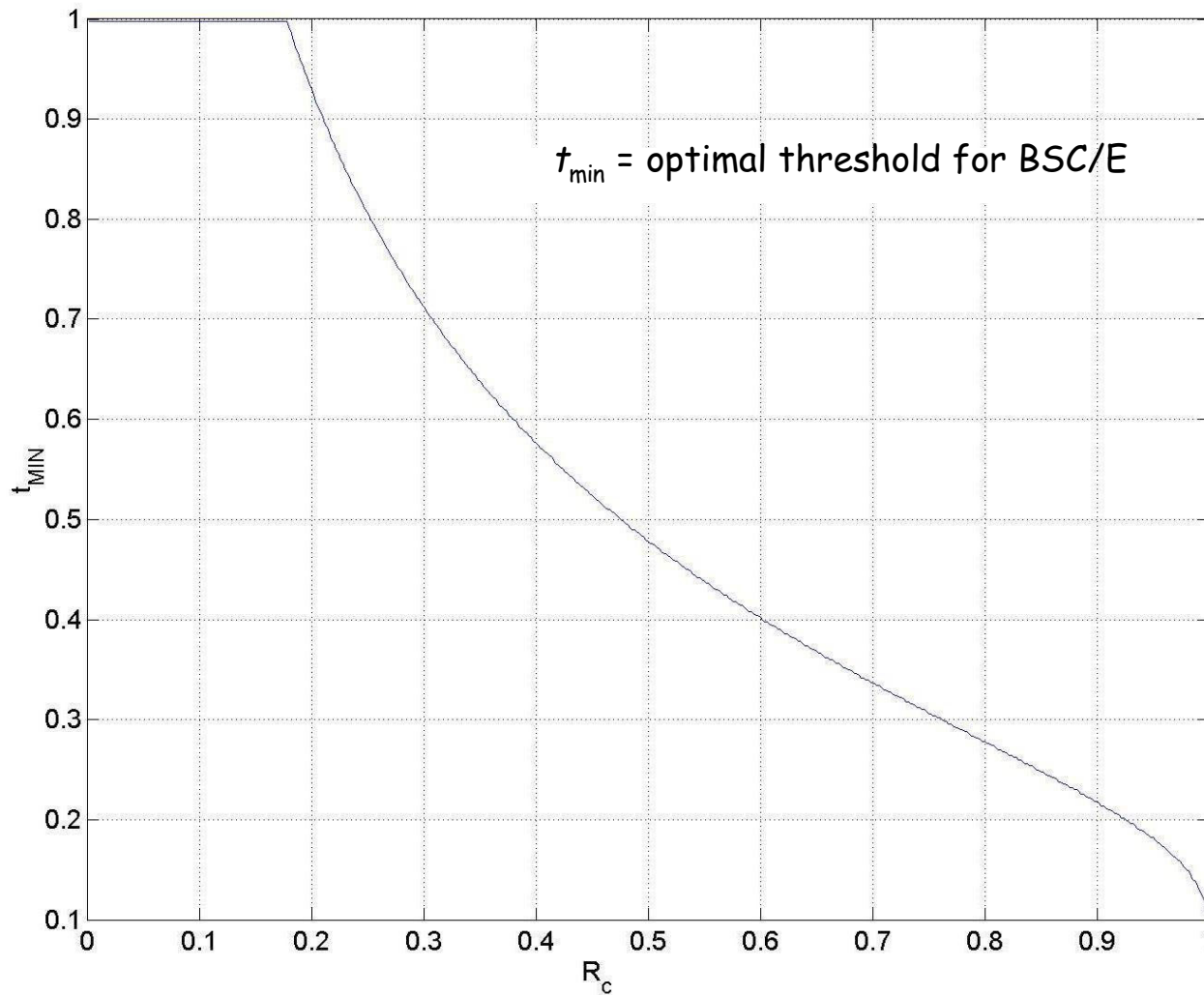
$$\beta_{avg} = \frac{1}{2} \left[ \frac{\mu_0^2}{\sigma_0^2} + \frac{\mu_1^2}{\sigma_1^2} \right] = \frac{2M^2 + 4\beta M + \beta^2}{2M + 4\beta}$$



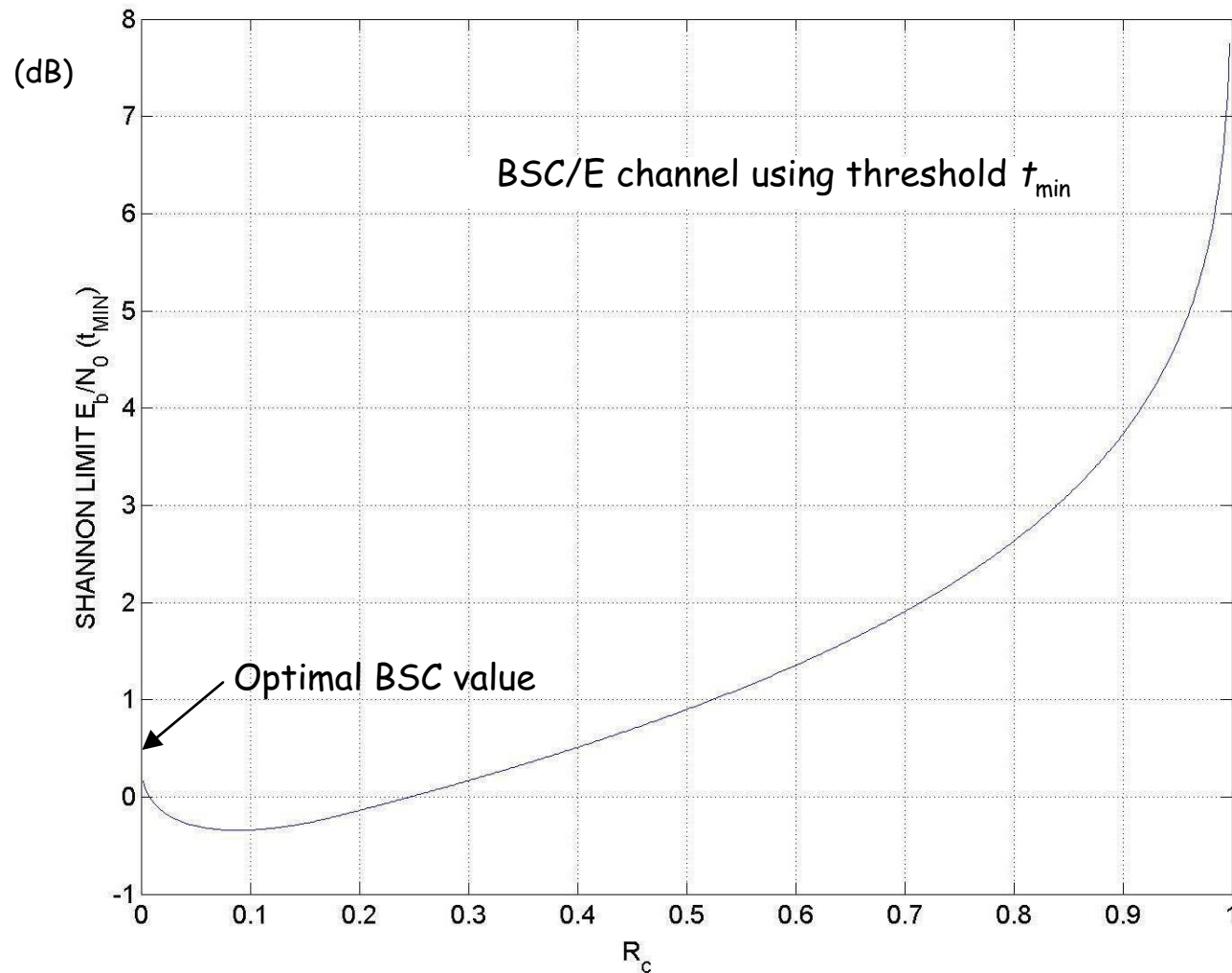
# BAC Shannon limit of $\beta$ and $Q$ vs $R_c$ for various $M$



# Optimal threshold $t_{\min}$ vs $R_c$ for BSC/E channel



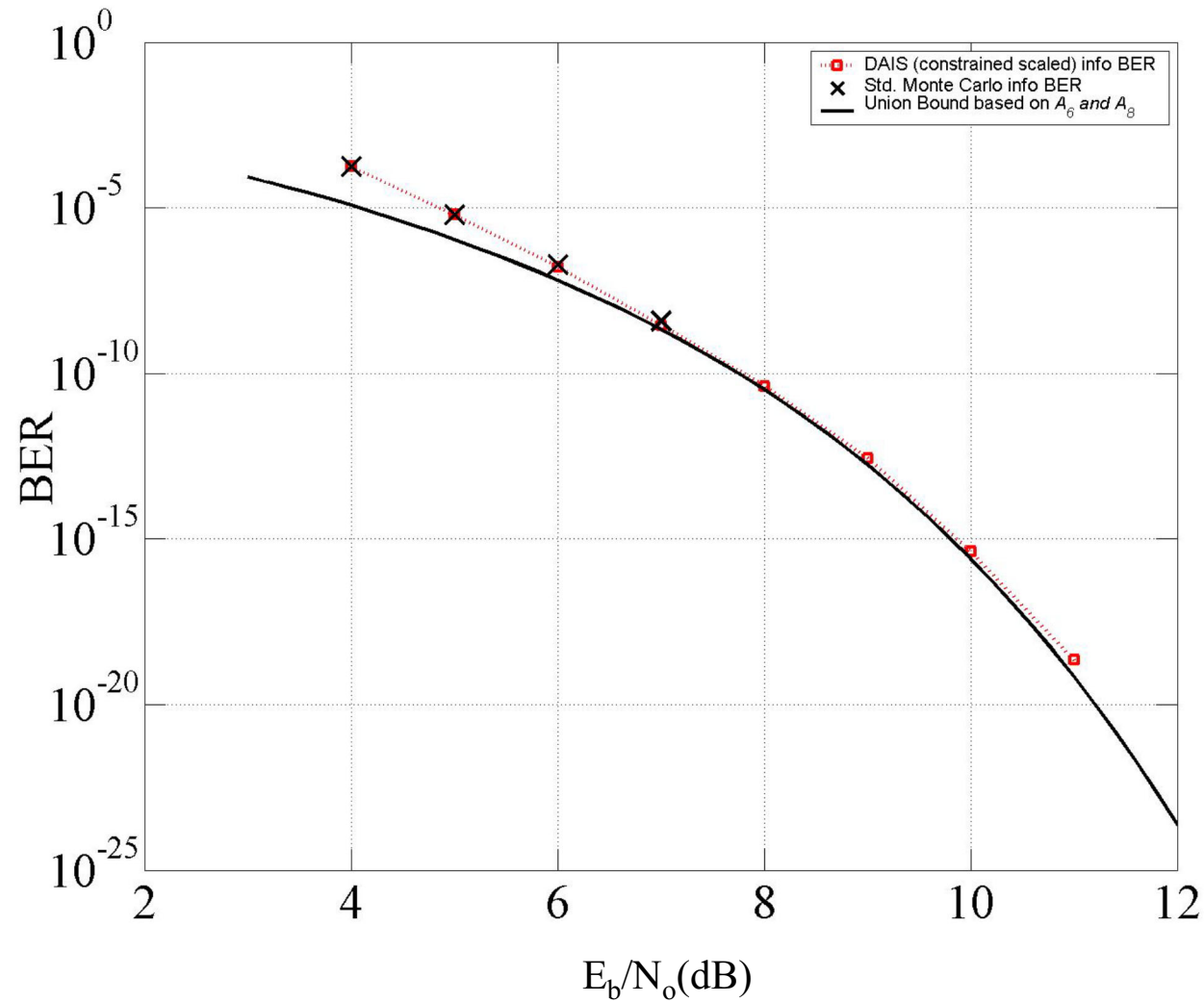
# Shannon limit $E_b/N_0$ vs $R_c$ using $t_{\min}$ for BSC/E channel



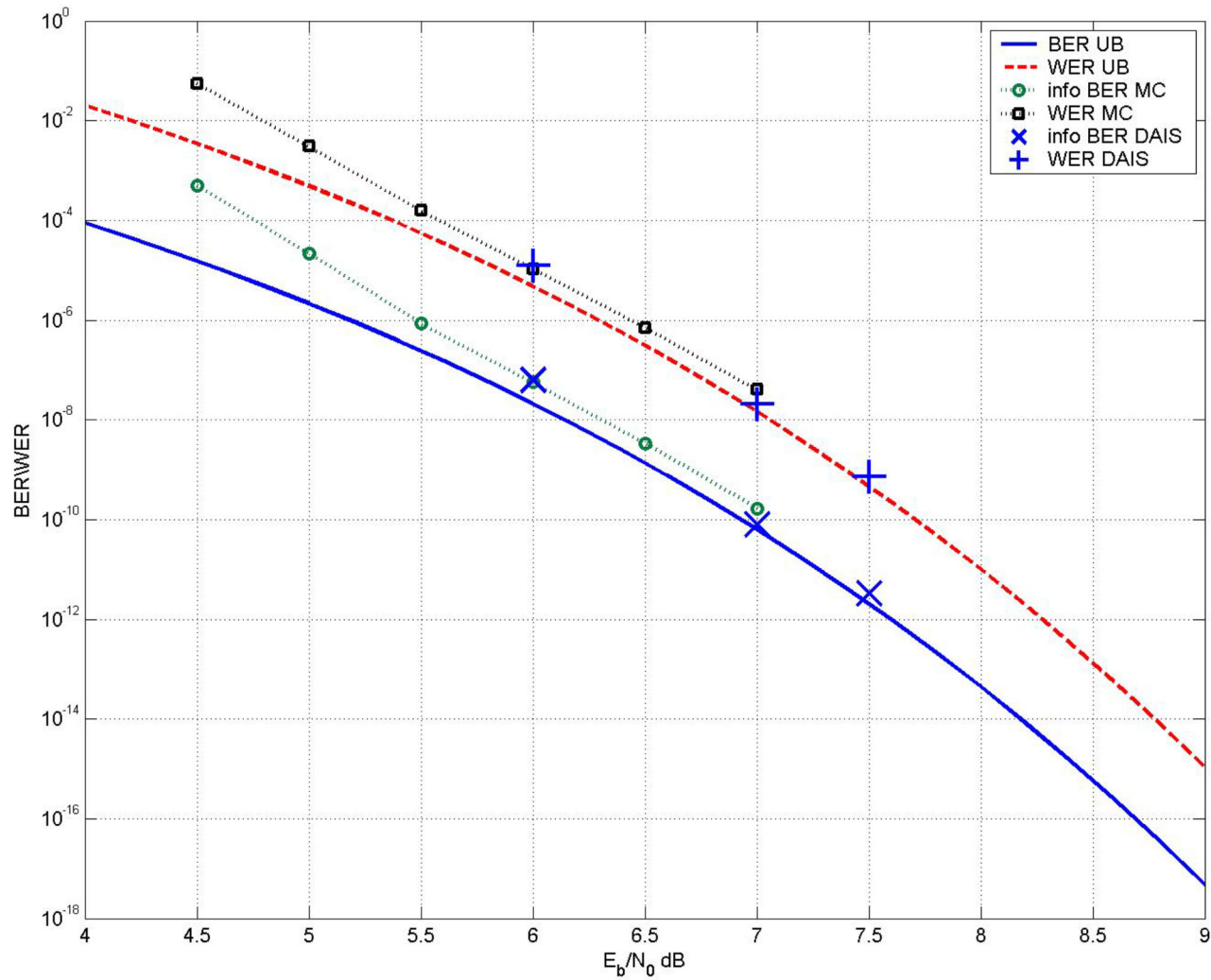
# Evaluations

- Sensitivity of SPA decoding of LDPC codes to noise  $\sigma^2$  variations
- $P_{DWC}$  as a lower bound on WER for class of hard decision decoders for BSC
  - ➔ extendable to soft-decision decoding
- DAIS ~ joint development of adaptive IS algorithms & software for simulation evaluation of FEC systems at very low BERs
  - AWGN-BPSK channel initially
  - Conceptually extendable to other channel models
  - Provisional patent application obtained

## BER for (96,50) LDPC code under SPA decoding via DAIS



## WER/BER for $\eta = 37$ RCD code under SPA decoding via DAIS



## Papers, Presentations, Dissertations, etc.

Mamtora, D., Mahadevan, A., and Morris, J. M., "A Performance Surface Characterizing Sensitivity to Incorrect Channel Noise Statistics for SPA Decoding of LDPC Codes for M-QAM", *Proc. 3<sup>rd</sup> Int'l. Symp. Turbo Codes and Related Topics*, Brest, France, 1-5 Sept. 2003, pp. 559-562.

Martin, W. and Morris, J. M., "The RCD Array Code is a Weakly Random-Like Code", *Proc. 3<sup>rd</sup> Int'l. Symp. Turbo Codes and Related Topics*, Brest, France, 1-5 Sept. 2003, pp. 351-354.

William R. Martin, "The Weight Enumerator Function for the RCD Array Codes: A Class of LDPC Codes", Ph.D. Dissertation, CSEE Dept/UMBC, Dec. 2003.

Mahadevan, A. and Morris, J. M., "On the Bounded-Distance Decoder's Probability of Decoding to a Wrong Codeword as a Lower Bound on WER for a Class of Decoders", submitted to *IEEE Trans. Information Theory*, 2004.

Mahadevan, A. and Morris, J. M., "On Minimum-WER Performance of FEC Codes for the BSC/E Based on BPSK-AWGN Under Extended Bounded Distance Decoding", submitted to *IEEE Trans. Communications*, 2004.

R. Holzlöhner, A. Mahadevan, C. R. Menyuk, J. M. Morris, and J. Zweck, "Evaluation of the Very Low BER of FEC Codes Using Dual Adaptive Importance Sampling", to appear *IEEE Communication Letters*, 2004.

Amitkumar Mahadevan., "On RCD Codes as a Class of LDPC Codes: Properties, Decoding, and Performance Evaluation", PhD Dissertation, CSEE Dept/UMBC, Dec. 2004 (expected).

\_\_\_\_, Mahadevan, A., Menyuk, C. R., Morris, J. M., \_\_\_\_\_, "Dual Adaptive Importance-Sampling Technique for Estimating Probabilities of Very Rare Events in Coded Communication Systems", Provisional Patent Application #60/486,970, 14 July 2003.



# Proposed Future Topics

- Extension of RCD codes to codes having  $\geq 4$  slope (diagonal) sets
- Hardware (FPGA) implementation of BFA, and test via Carter's testbed
- $P_{DWC}$  as WER lower bound for soft-decision decoders
- Additional channel models with erasures (2-thresholds): **BAC/SE & BSC/AE**
- Channel models incorporating DPSK modulation/demodulation
- DAIS used for sensitivity studies & non-BSC channel models
- DAIS patent & further development for commercial licensing
- Quantum channel models and error correction