



# Time-Step Network Simulation

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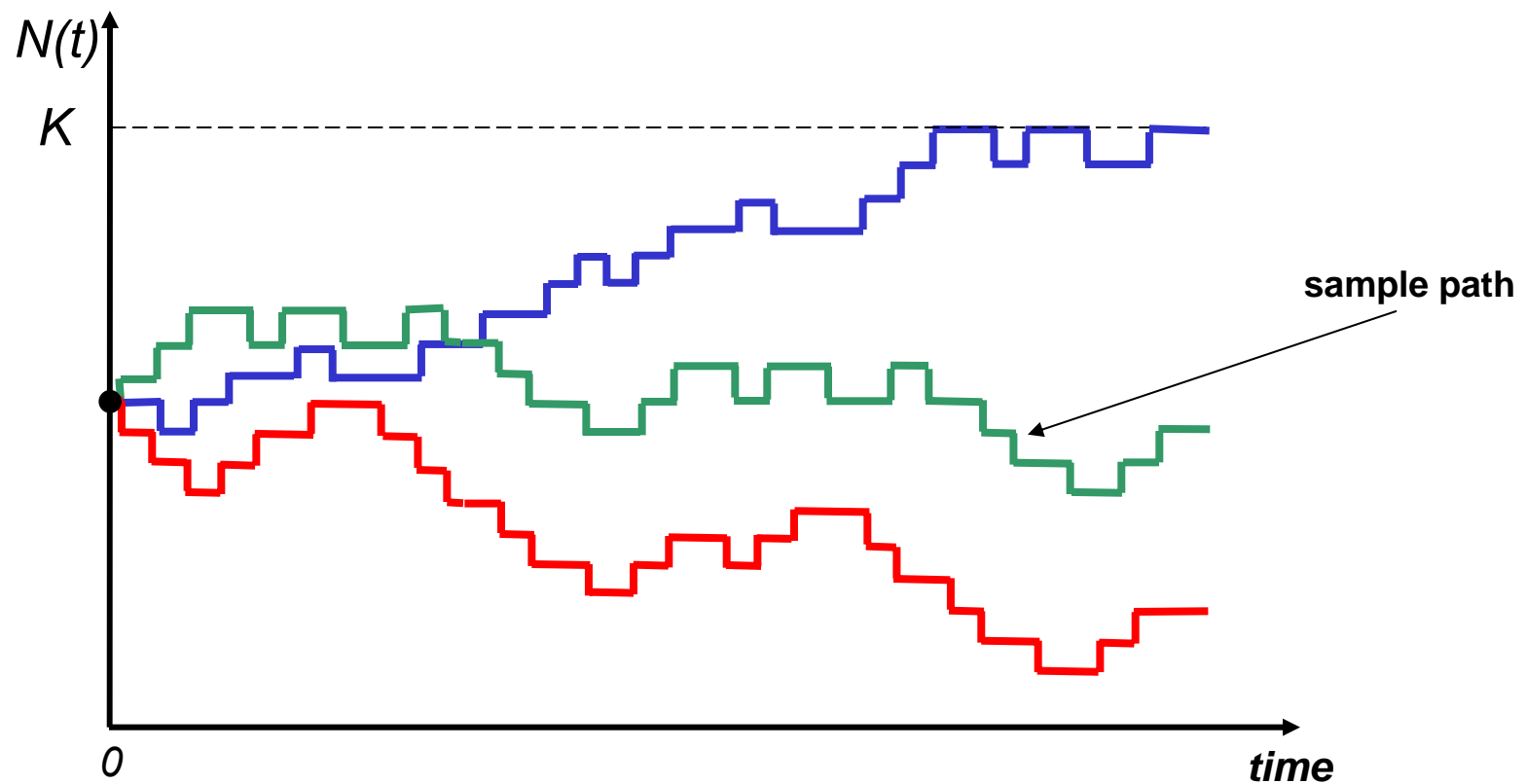
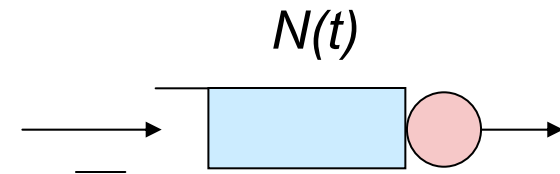
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# Introduction

- Goal: Fast accurate performance evaluation tool for computer networks
  - Handles general control schemes (time- and state-dependent)
- Packet-level simulation:
  - Handles general control scheme precisely but prohibitively expensive
- Steady-state exact queuing models
  - Handles only simple models; no transient metrics
- Time-dependent exact queuing model
  - Only very simple systems; no state-dependent control
- Time-dependent stochastic model (fluid and diffusion approximations)
  - Handles time-dependent, but not state-dependent control
- Approach: Combine discrete-event simulation with diffusion approximation
  - Accurate, inexpensive, handles time- and state-dependent control

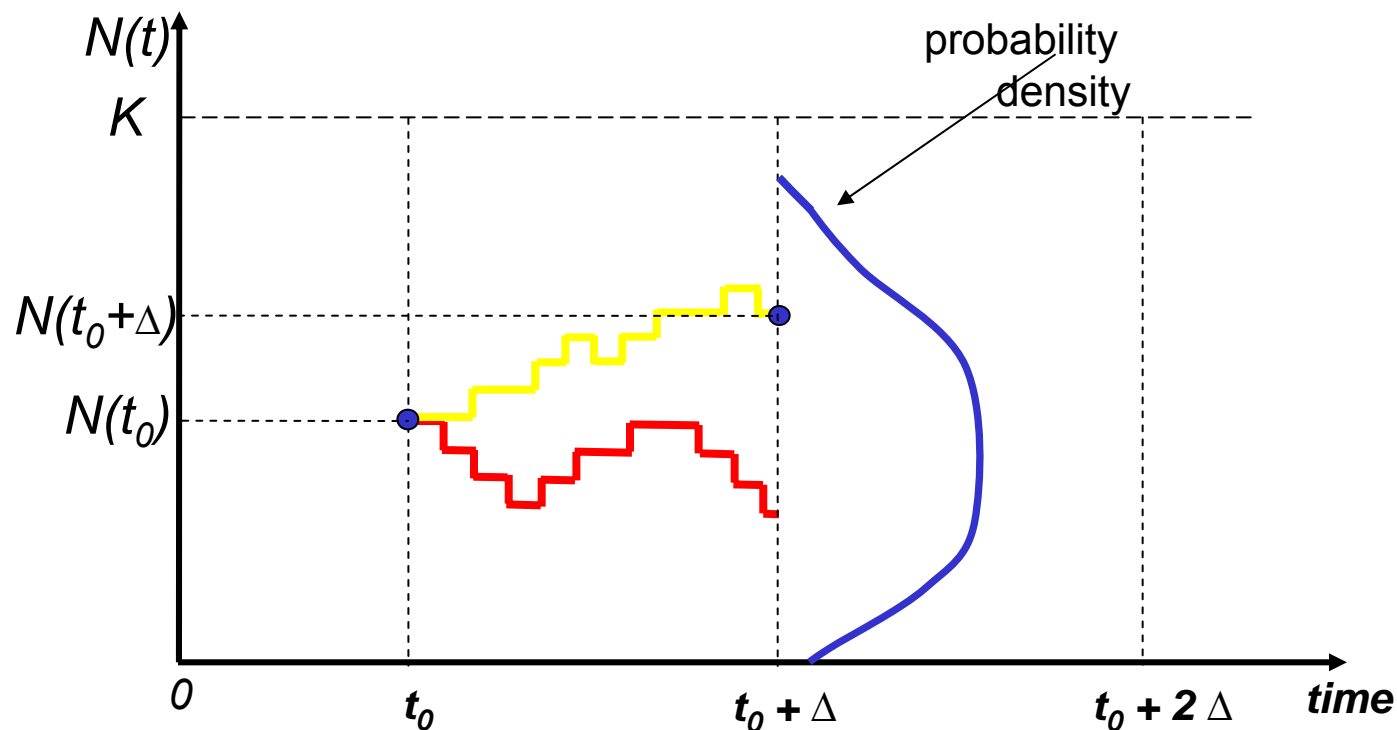
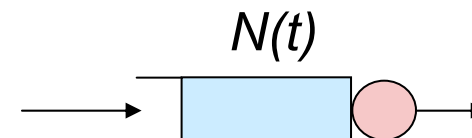
# Hybrid time-step simulation

- Consider a single communication link
- Want to generate sample paths efficiently



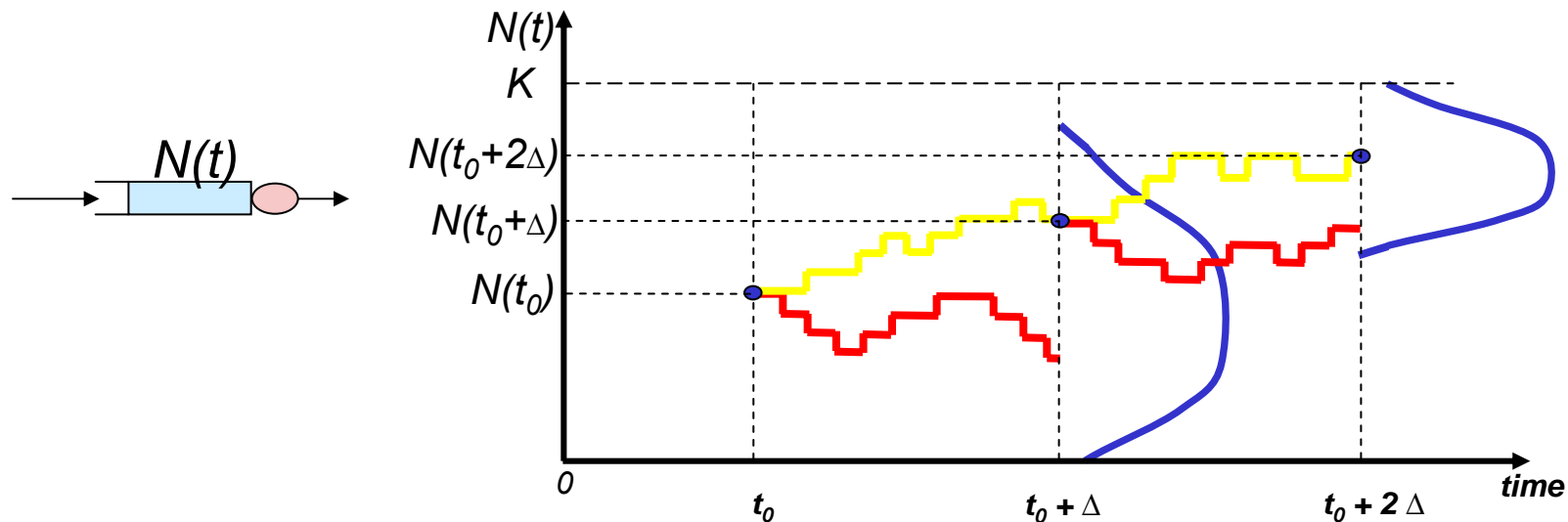
# Hybrid time-step simulation

- Divide time axis into small intervals  $\Delta$
- For interval  $[t_0, t_0 + \Delta]$  choose  $N(t_0 + \Delta)$  randomly based on  $N(t_0)$  and arrival and service processes
- Repeat for successive time intervals



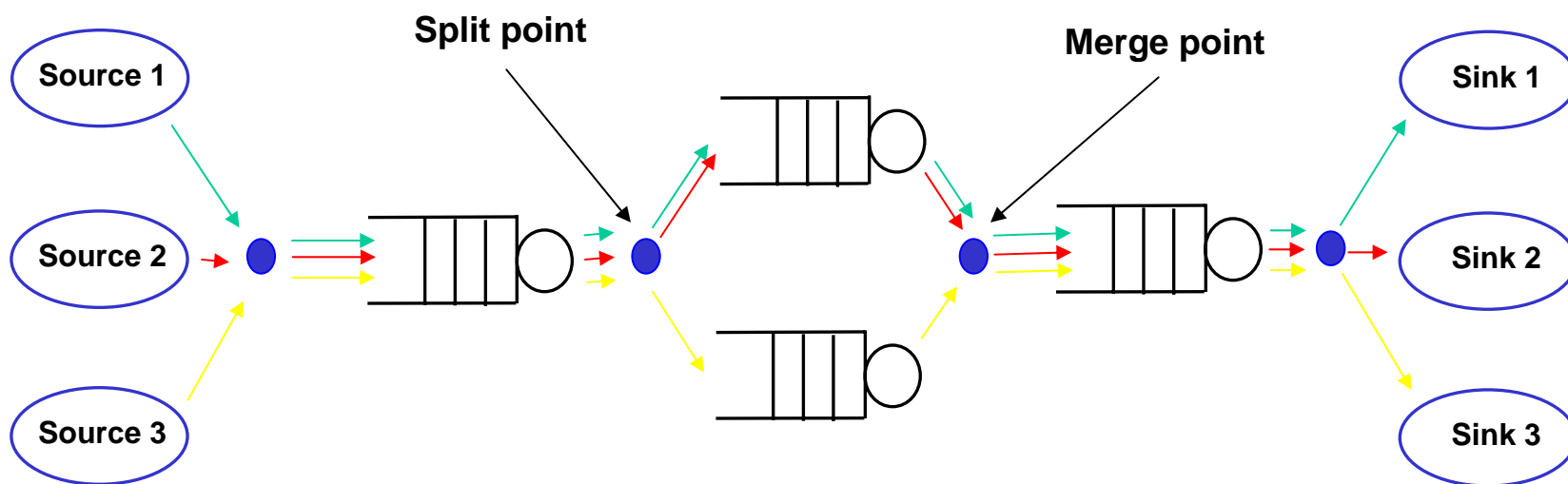
# Hybrid time-step simulation

- Time/state dependent sources undergo state changes at every  $\Delta$  ( $\Delta \approx$  time scale of upper-layer control, e.g., RTT for TCP)
- Discrete events are not packet transmissions but time steps
- Captures state-dependent control because sample-path is explicit
- Diffusion approximation [Kolomogorov] to obtain  $\text{Prob}[ N(t+\Delta) | N(t) ]$ 
  - Arrival and service processes defined by time-varying mean and variance



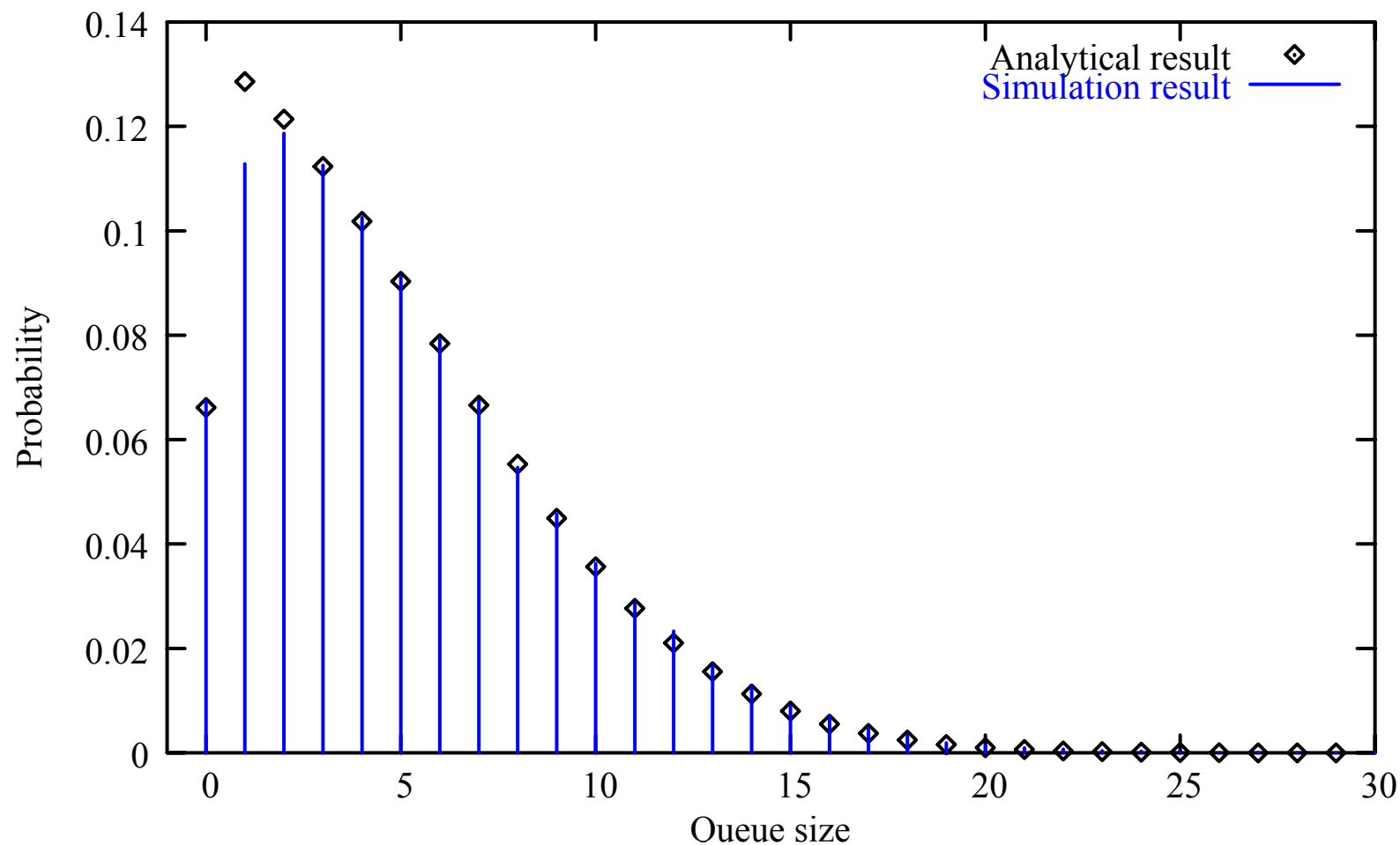
## Extension to network of queues

- For each interval  $[t, t + \Delta]$ 
  - Approximate queue departure and internal flows by renewal processes characterized by the first two moments
  - Routing probabilities determined by queue occupancy
- Formulate equations for merging and splitting flows



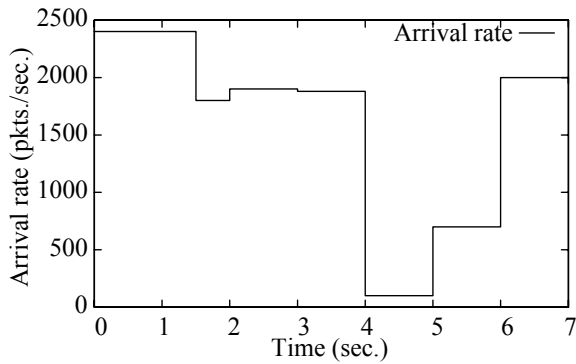
## Example: Queue size prob density

- GI/D/1/40 queue,  $\lambda=800$ ,  $c_A=1$ , and  $\mu=810$ ,  $N(t) = 2$ ,  $\Delta=0.05$

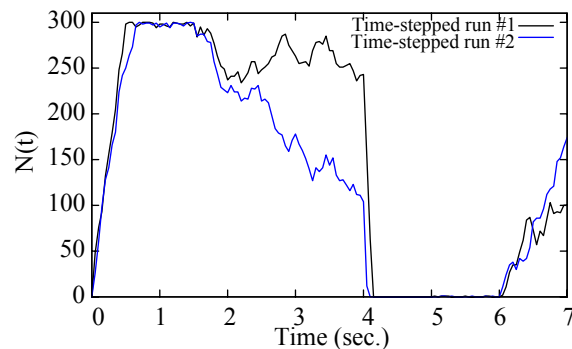
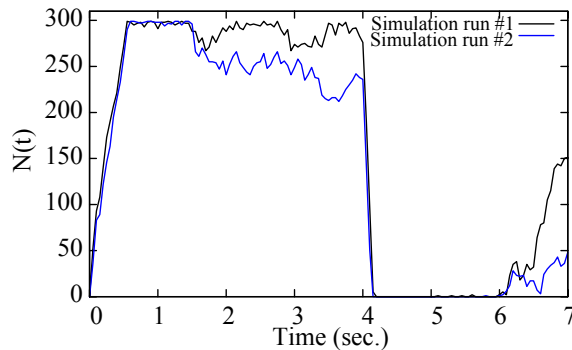


# TSS

## Example: TSS vs. packet-level simulation

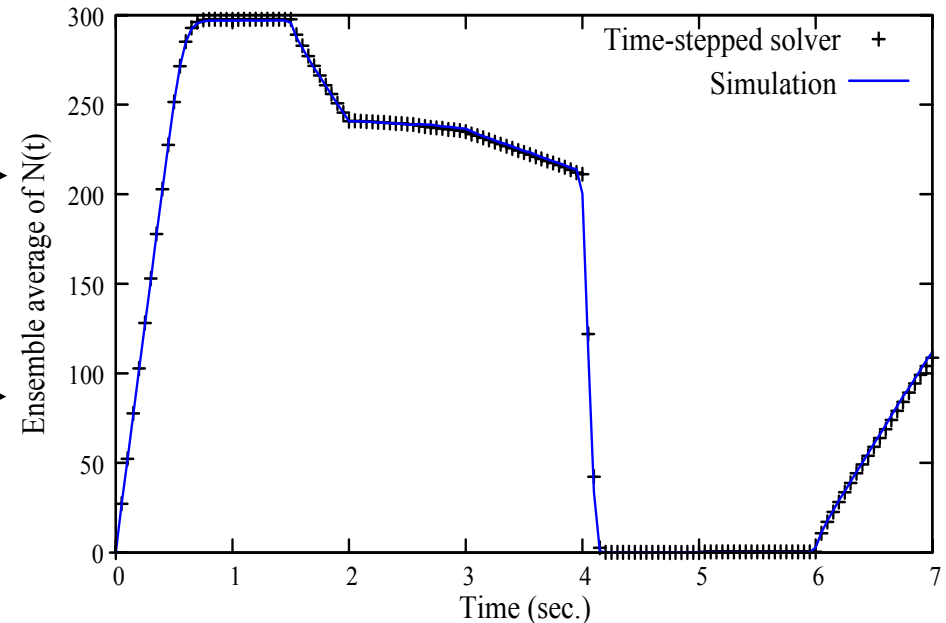


- GI(t)/D/1/300 queue, uniform arrival dist,  $\mu=1900$
- Computation time of one run:
  - 10 Mbps link - simulation 1.5 sec., hybrid 0.1 sec.
  - 100 Mbps link - simulation 15 sec., hybrid 0.1 sec.
- Time-step simulator converges faster due to smaller probability space



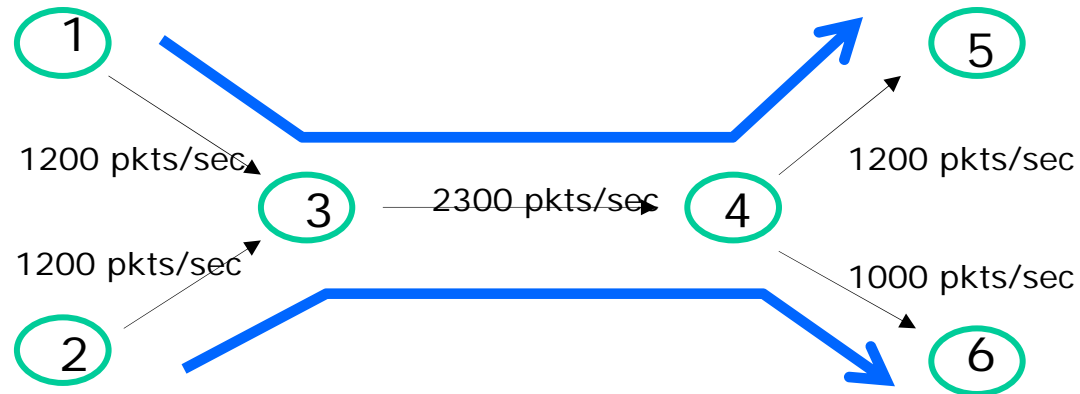
1K runs

100 runs





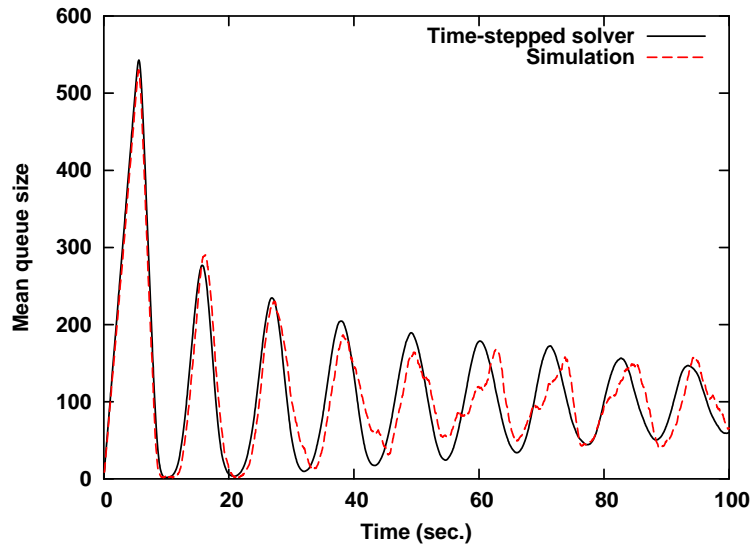
## Example: Network with state-dependent traffic sources



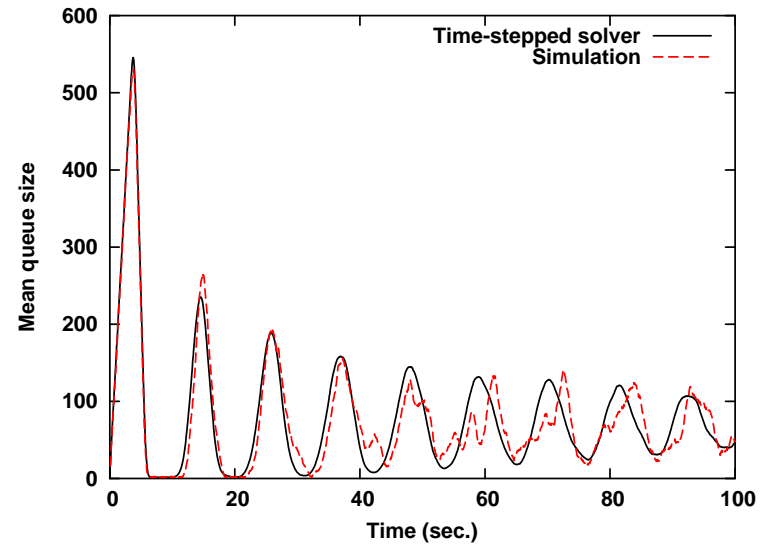
- Traffic flows 1→5 and 2→6 sharing link 3→4.
- Each traffic source:
  - Starts at 1350 pkts/sec
  - 900 pkts/sec when  $RTT > 1.0$  sec
  - 1350 pkts/sec when  $RTT < 0.5$  sec
  - Squared coefficient of variation 1.0
- Service:
  - forward rates as shown above
  - backward rates are all 20000 pkts/sec
  - Squared coefficient of variation of service of all links is 0.0



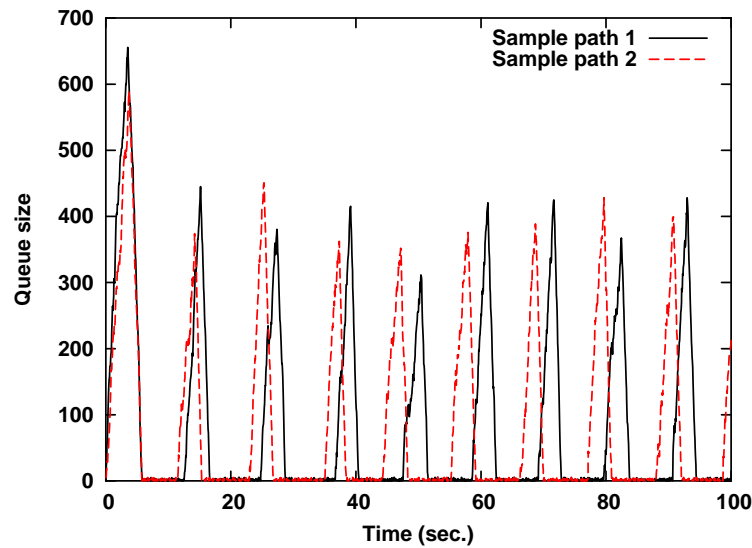
# Example: Network with state-dependent traffic sources



Mean queue size of link 3 → 4



Mean queue size of link 2 → 3



Sample paths of queue size of link 2 → 3

## Model of the TCP flow (generalized AIMD)

- Congestion window  $cwnd(t)$  for time interval  $[t, t + \Delta]$  based on  $RTT$  and history
- Send rate of source in interval  $[t, t + \Delta]$  is:

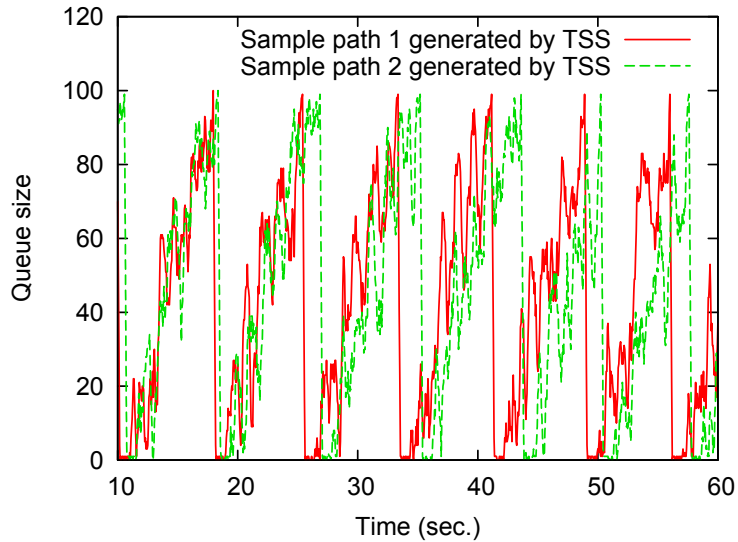
$$sndRate(t) = cwnd(t) / rtt$$

- Loss count in interval  $[t, t + \Delta]$  based on probability  $p$  of being at the upper boundary:

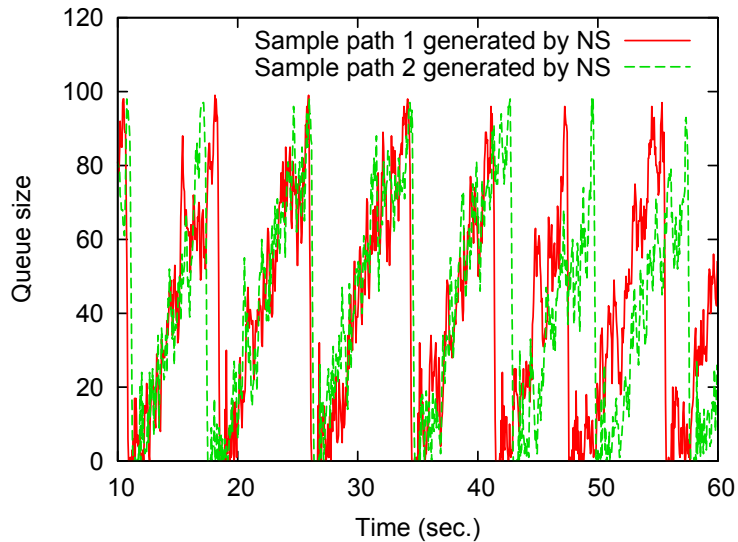
$$lossCount(t) = arrRate(t) * \Delta * p$$

- Losses assigned to flows based on the ratio of arrival rates

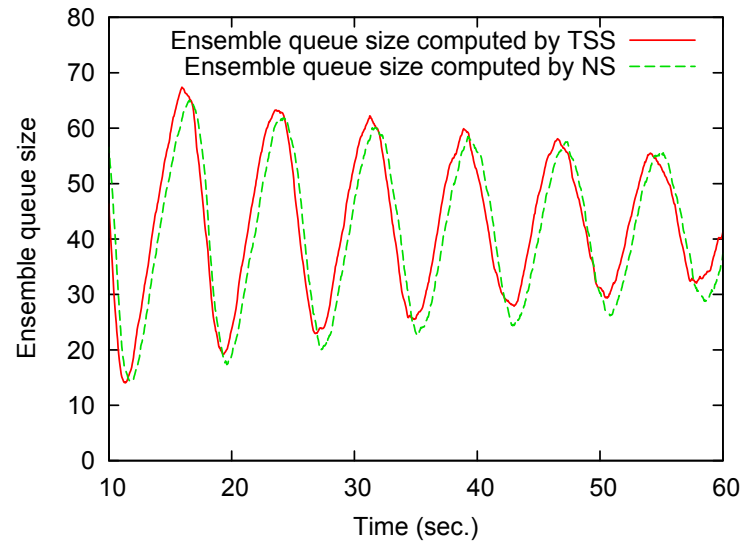
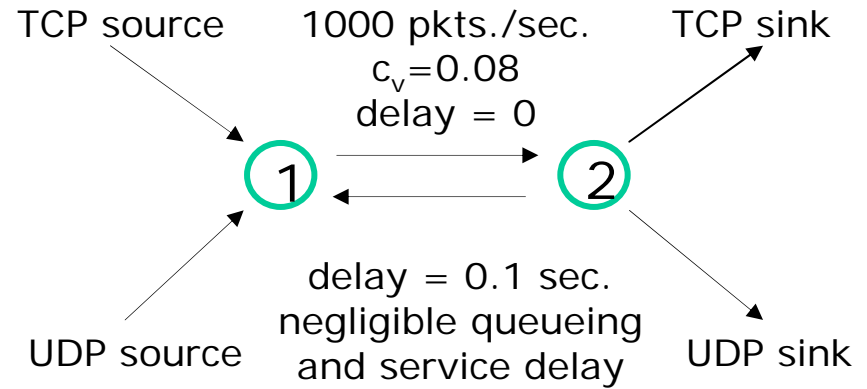
# Example: TCP and UDP sharing a link



TSS sample paths



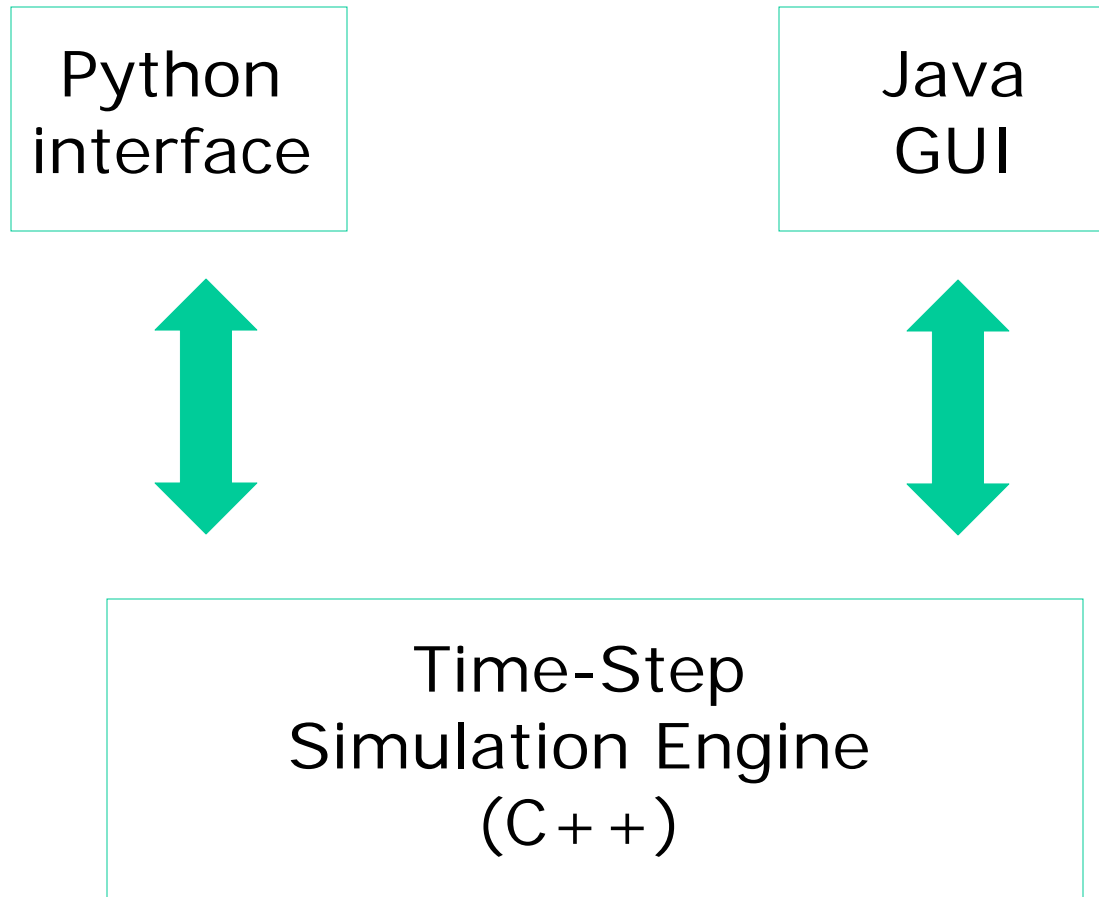
NS sample paths



mean queue size – TSS vs. NS

TSS

# Software architecture



TSS

## Simulation script - example

```
runTime = 400  
nrRuns = 2000
```



**set parameters**

```
N = Network()  
N.addNode(1)  
N.addNode(2)  
N.addLink(0, 1, 2, 2000, 1200, 0.05, 0, 0)  
N.addLink(1, 2, 1, 300, 10000, 0.1, 0, 0)
```



**define topology**

```
N.addFlow(1, "TCP", "", 1, 2, 0, 10)
```



**define flows**

```
N.initSolver()  
time = 0  
while time <= runTime:  
    log_links(N, time)  
    time = N.makeStep()
```



**run simulation**

# Time-step simulation - Conclusions

- Time-stepped simulation using diffusion approximation
- Fast and accurate alternative to packet-level (discrete-event) simulation
- Computational complexity not affected by increasing link bandwidth
- Handles state-dependent control schemes
- Yields time-dependent evolution of performance metrics
- Ongoing work
  - Extend queue model to handle wireless links (802.11)
  - Extend to other router disciplines (RED, AQM, CBQ)
  - Optimize numerical computation
  - Detailed comparisons against packet-level simulation for large networks